

## First derivative test for relative extrema

Suppose  $f$  is continuous on the interval  $(a, b)$ . Also suppose that  $f$  is differentiable on  $(a, b)$ , except possibly at some isolated points.

- If  $f'(x)$  changes from negative to positive at a critical number  $c$ , then  $f(c)$  is a relative minimum.
- If  $f'(x)$  changes from positive to negative at a critical number  $c$ , then  $f(c)$  is a relative maximum.
- If  $f'(x)$  has the same sign on both sides of a critical number  $c$ , then  $f(c)$  is neither a relative minimum nor a relative maximum.

## **Finding intervals on which $f$ is increasing/decreasing**

Suppose that  $f$  is continuous on the interval  $I$ . Also suppose that  $f$  is differentiable inside  $I$ , except possibly at some isolated points. We use the following steps to find the relative extrema and open intervals on which  $f$  is increasing/decreasing.

1. Determine domain endpoints (if any) and all points at which  $f'(x)$  is zero or not defined.
2. Draw a number line and mark the points found in step 1. (Indicate which are critical numbers.)
3. Determine the sign of  $f'(x)$  on each interval along your number line.
4. List open intervals on which  $f$  is increasing/decreasing.
5. Identify and list all relative extrema, including both  $x$ - and  $y$ -coordinates.