## Rolle's Theorem

Suppose $f$ is continuous on $[a, b]$ and differentiable on $(a, b)$. If $f(a)=f(b)$, then there exists a number $c$ in $(a, b)$ such that $f^{\prime}(c)=0$.

## Mean Value Theorem

If $f$ is continuous on $[a, b]$ and differentiable on $(a, b)$, then there exists a number $c$ in $(a, b)$ such that

$$
f^{\prime}(c)=\frac{f(b)-f(a)}{b-a} .
$$

## Increasing/decreasing functions - Definition

Suppose the function $f$ is defined on an interval $I$.

- If for any two points $x_{1}$ and $x_{2}$ in $I$,

$$
x_{1}<x_{2} \quad \Longrightarrow \quad f\left(x_{1}\right)<f\left(x_{2}\right),
$$

then $f$ is increasing on $I$.

- If for any two points $x_{1}$ and $x_{2}$ in $I$,

$$
x_{1}<x_{2} \quad \Longrightarrow \quad f\left(x_{1}\right)>f\left(x_{2}\right),
$$

then $f$ is decreasing on $I$.

## Increasing/decreasing functions - Theorem

If $f$ is differentiable at each point of $(a, b)$ and the derivative is positive at each point, then $f$ is increasing on $(a, b)$.

If $f$ is differentiable at each point of $(a, b)$ and the derivative is negative at each point, then $f$ is decreasing on $(a, b)$.

