

Math 200 - Quiz 6

February 29, 2012

Name key

Score _____

Show all work to receive full credit. Supply explanations when necessary.

1. (1 point) State one of the important properties of the Hindu-Arabic numeration system.

① EACH NUMERAL IS CONSTRUCTED USING 10 BASIC DIGITS: 0, 1, 2, 3, 4, 5, 6,
7, 8, 9

② PLACE VALUE IS BASED ON POWERS OF 10: $10^0, 10^1, 10^2, \dots$

2. (1 point) Find the base-ten equivalent of the base-five numeral 342_{five} .

$$\begin{aligned} & 3 \times 5^2 + 4 \times 5^1 + 2 \times 5^0 \\ &= 3 \times 25 + 4 \times 5 + 2 \\ &= 75 + 20 + 2 = \boxed{97_{\text{TEN}}} \end{aligned}$$

3. (1 point) List the first 10 natural numbers in base three.

$$1, 2, 10, 11, 12, 20, 21, 22, 100, 101, \dots$$

ALL IN BASE THREE

4. (2 points) Find the base-seven equivalent of the base-ten numeral 1842.

$$7^0 = 1, 7^1 = 7, 7^2 = 49, 7^3 = 343, 7^4 = 2401$$

$$7^3 = 343 \overline{)1842} \quad 5$$

$$7^2 = 49 \overline{)127} \quad 2$$

$$7^1 = 7 \overline{)29} \quad 4$$

$$7^0 = 1 \overline{)1} \quad 1$$

$$1842_{\text{TEN}} = \boxed{5241_{\text{SEVEN}}}$$