

Math 112 - Test 1
February 7, 2018

Name _____

Score _____

Show all work. Supply explanations when necessary. Partial credit will be awarded for correct work.

1. (3 points) Write the following set in set-builder notation.

{January, June, July}

2. (3 points) Give a verbal description of the elements of the set $\{5, 10, 15, 20, \dots\}$.

3. (4 points) Rewrite the set S in roster notation.

$$S = \{x \mid x \in \mathbb{N} \text{ and } 1 \leq x < 7\}$$

4. (5 points) Decide if each statement is true (T) or false (F).

(a) _____ $3.14159 \in \mathbb{N}$

(b) _____ $\{1, 2, 3, 4\} \subseteq \{2, 4\}$

(c) _____ $\text{Chicago} \in \{x \mid x \text{ is one of the United States}\}$

(d) _____ $n(\mathbb{N}) = \infty$

(e) _____ $\emptyset \subseteq \{a, b, c, d, \dots, y, z\}$

5. (4 points) Suppose we are thinking about the set of all patients at a doctor's office who have waited a long time to be seen. Is this set well defined? Explain why or why not.

6. (2 points) Give a subset of $\{w, x, y, z\}$ that is **NOT** a proper subset.

7. (6 points) Let A be the set of letters of the word *ILLINOIS*.

(a) Write A in roster notation.

(b) Determine $n(A)$.

(c) Give an example of a set that is equivalent to A , but not equal to A .

8. (5 points) For each pair of sets, determine whether they are equal, equivalent, or neither. **Circle all that apply.**

(a) $\{s, t, u, v, w\}$ $\{t, v, w, s, u\}$ Equal Equivalent Neither

(b) $\{1, 2, 3, 4, 5, 6\}$ $\{2, 4, 6, 8, 10, 12\}$ Equal Equivalent Neither

(c) $\{\text{five}\}$ $\{\text{f, i, v, e}\}$ Equal Equivalent Neither

9. (1 point) Which one of the following sets is NOT empty?
- (a) The set of all even numbers in $\{1, 3, 5, 7, 9, \dots\}$
 - (b) \emptyset
 - (c) The set of all natural numbers less than 1
 - (d) $\{\emptyset\}$
10. (1 point) Which one of the statements below would be read “A is equivalent to B?”
- (a) $A \subseteq B$
 - (b) $A \in B$
 - (c) $A \cong B$
 - (d) $B = \{x \mid x \in A\}$
11. (1 point) For which one of these sets is it true that $n(C) = 1$?
- (a) $C = \emptyset$
 - (b) $C = \{0, 1\}$
 - (c) $C = \{\emptyset\}$
 - (d) $C = \{1, 10, 100, 1000, \dots\}$
12. (1 point) Let $Z = \{a, b, c\}$. Which one of these sets is NOT a proper subset of Z ?
- (a) \emptyset
 - (b) $\{a\}$
 - (c) $\{a, b\}$
 - (d) $\{a, b, c\}$
13. (1 point) Let $A = \{1, 3, 5, 7\}$. How many subsets does A have?
- (a) 4
 - (b) 8
 - (c) 15
 - (d) 16

14. (4 points) Suppose U is the set of all PSC students, and M is the subset of math students. Using words, describe the elements of M' .

15. (16 points) Let $V = \{a, e, i\}$ and $W = \{a, b, c, d, e\}$, and consider V and W as subsets of the universal set $U = \{a, b, c, d, e, f, g, h, i\}$. Determine each of the following.

(a) $n(W)$

(b) V'

(c) $W \cup V$

(d) $W' \cap V$

(e) $(V \cap W)'$

(f) $W \cup \emptyset$

(g) $V - W$

(h) $V \cap \emptyset$

16. (5 points) Let $U = \{11, 12, 13, 14, 15, 16, 17, 18, 19, 20\}$ and think about the following subsets: $A = \{14, 15, 16, 17\}$, $B = \{11, 13, 15, 17, 19\}$, $C = \{12, 14, 15, 19, 20\}$. Determine the set $(B \cup C) \cap A'$.

17. (6 points) Let L be the set of letters of the word *racecar* and let $T = \{a, b\}$.

(a) Determine the Cartesian product $T \times L$.

(b) Determine the difference $L - T$.

18. (6 points) Rewrite each of the following statements or phrases using mathematical notation.

(a) The intersection of the sets X and Y

(b) The set A is equivalent to the set B .

(c) 5 is not an element of the set Q .

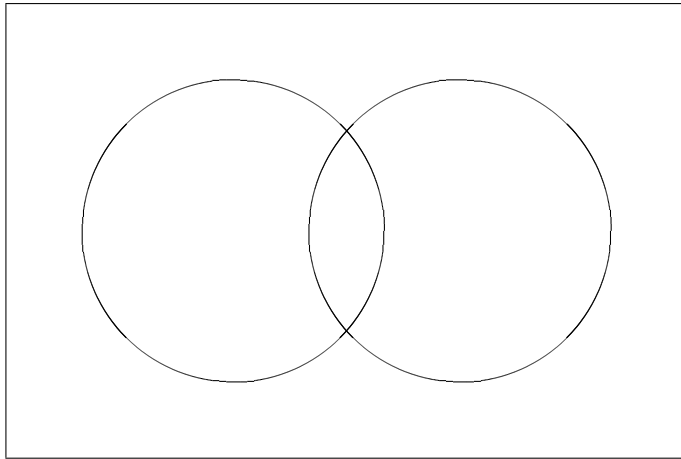
(d) The cardinality of the union of the two sets P and Q is 13.

(e) The set G is a proper subset of the set H .

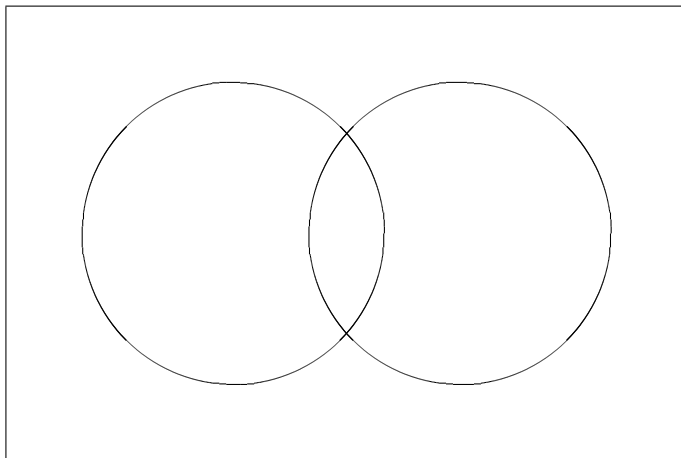
(f) The set D is the empty set.

19. (8 points) Label the sets A and B , then shade the region corresponding to each given set operation. Show work or explain your reasoning.

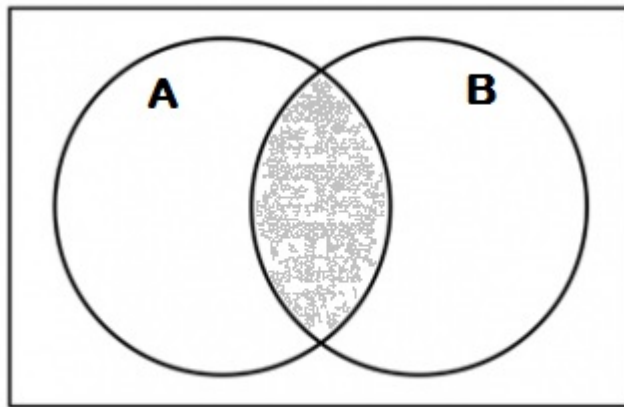
(a) $A \cup B$



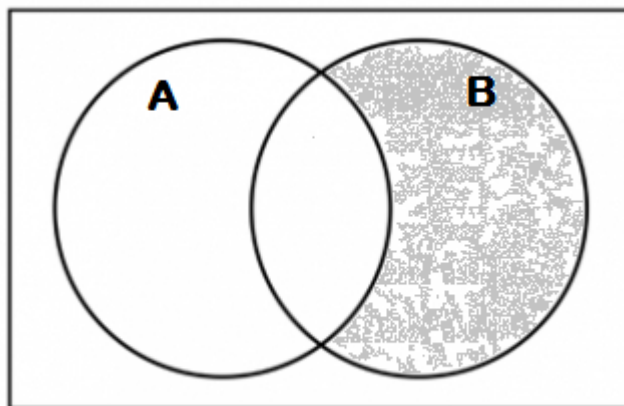
(b) $A \cap B'$



20. (8 points) Use set notation to name the shaded region.



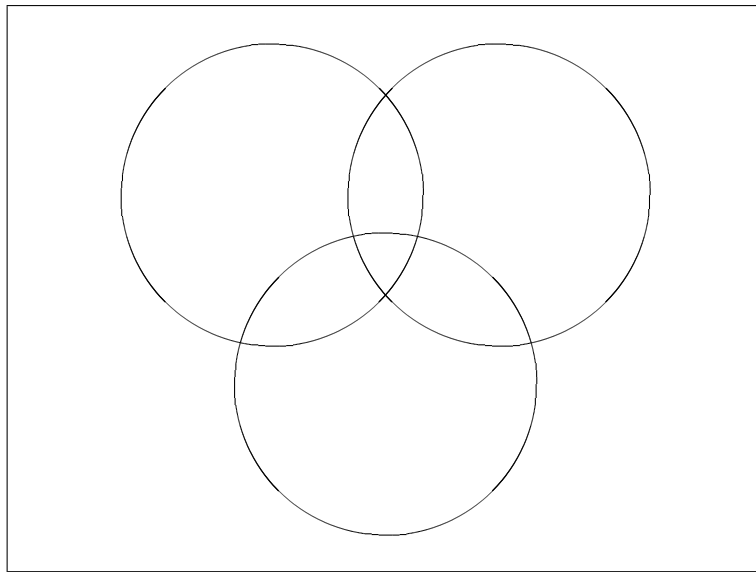
(a)



(b)

21. (10 points) Label the sets A , B , and C , then shade the region corresponding to each given set operation. Show work or explain your reasoning.

(a) $(A \cap B) \cup C$



(b) $(A - B) \cap C$

