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Show all work. Supply explanations when necessary. Partial credit will be awarded for correct work.

1. (6 points) Write each set in roster notation.
(a) $A$ is the set of counting numbers less than 6 .
(b) $Q$ is the set of letters of the word sleeplessness.
(c) $D=\{s \mid s \in \mathbb{N}$ and $6<s<10\}$
2. (2 points) The set of heart failure patients who deserve heart transplants is not well defined. Give one reason for why not.
3. (3 points) The following set is described in set-builder notation. Translate this description word for word into a complete sentence.

$$
B=\{x \mid x \in \mathbb{N} \text { and } x<10\}
$$

4. (4 points) Give a verbal description of each set.
(a) $\{10,12,14,16, \ldots, 48\}$
(b) $\{a, u, g, s, t\}$
5. (2 points) Write the set $M=\{1,2,3,4, \ldots, 100\}$ in set-builder notation.
6. (5 points) Decide whether each statement is true or false.
(a) $\qquad$ $79 \in\{1,3,5,7,9,11, \ldots\}$
(b) $\qquad$ $-5 \in \mathbb{N}$
(c) $\qquad$ $\{r \mid r \in \mathbb{N}$ and $r+1=0\}$ is the empty set.
(d) $\qquad$ $\{k \mid k \in \mathbb{N}$ and $k-1=0\}$ is the empty set.
(e) $\qquad$ Homewood $\in\{x \mid x$ is one of the United States $\}$
7. (5 points) Determine the cardinal number for each set.
(a) $\qquad$ $A=\{2,4,6,8,10\}$
(b) $\qquad$ $B=$ the set of letters of the word didgeridoo
(c) $\qquad$ $C=\{\emptyset\}$
(d) $\qquad$ $B=\{$ four $\}$
(e) $\qquad$ $E=\mathbb{N}$
8. (2 points) Give an example of a set that is equivalent to, but not equal to, $\{1,2,3,4\}$.
9. (4 points) List all subsets of the set $\{1,2,3\}$.
10. (4 points) Decide whether each statement is true or false.
(a) $\qquad$ $\{3\} \cong\{\emptyset\}$
(b) All equal sets are equivalent.
(c) $\qquad$ All equivalent sets are equal.
(d) $\qquad$ $\{1,2,3,4,5\} \cong\{10,20,30,40,50\}$
11. (1 point) Let $A=\{d, o, g\}$. Which one of these sets is NOT a proper subset of $A$ ?
(a) $\{d\}$
(b) $\{d, o, g\}$
(c) $\{d, g\}$
(d) $\emptyset$
12. (1 point) Let $C=\{1,2,3,4,5,6,7\}$. How many subsets does $C$ have?
(a) 7
(b) 100
(c) 128
(d) 150
13. (1 point) Which one of these sets is equivalent to $\{a, b, c\}$ ?
(a) $\{a b c\}$
(b) $\{123\}$
(c) $\{1,2,3\}$
(d) $\emptyset$
14. (1 point) Suppose $A$ and $B$ are NOT empty sets. Which one of the following sets IS empty?
(a) $\{\emptyset\}$
(b) $A \cup B$
(c) $B \cap B^{\prime}$
(d) $A \cup B \cup \emptyset$
15. (1 point) Let $A=\{1,2\}$ and $B=\{a, b, c\}$. Which one of these is an element of $A \times B$ ?
(a) $\{1,2, a, b, c\}$
(b) $\{1, b\}$
(c) $(1,1)$
(d) $(2, c)$
16. (16 points) Let $U$ be the set of letters of the English alphabet and think about the subsets $A=\{a, b, c, d, e\}$ and $B=\{a, e, i, o, u\}$. Determine each of the following.
(a) $n(B)$
(b) $A^{\prime}$
(c) $A \cup B$
(d) $A \cap B$
(e) $A \cap B^{\prime}$
(f) $A-B$
(g) $\emptyset \cup B$
(h) $A \cap \emptyset$
17. (6 points) Suppose $U$ is the set of dogs at the local animal shelter. Let $G$ be the subset of gray dogs and let $H$ be the subset of dogs weighing more than 50 lbs .
(a) How would you describe the elements of $G \cap H$ ?
(b) How would you describe the elements of $G^{\prime}$ ?
18. (6 points) In the two-set Venn diagram shown below, label the sets $A$ and $B$. Then label the four distinct (disjoint) regions with Roman numerals. Identify and shade the regions that make up $B-A$.

19. (8 points) Suppose $n(A)=53, n(B)=31, n(A \cap B)=17$, and $n(U)=80$. Use a Venn diagram to sort the data. Then determine $n(A \cup B)$.
20. (8 points) In the three-set Venn diagram shown below, label the sets $A, B$, and $C$. Then label the distinct (disjoint) regions of the diagram with Roman numerals. Identify and shade the regions that make up $A^{\prime} \cap(B \cup C)$.

21. (6 points) Rewrite each of the following statements using mathematical symbols.
(a) $A$ is a subset of $B$.
(b) The cardinal number of $D$ is 10 .
(c) $a$ is an element of the complement of the set $Q$.
22. (8 points) Out of 30 students taking an exam, 17 answered the first bonus question (Q1), 19 answered the second bonus question (Q2), and 6 did not attempt either of the two bonus questions. Use a Venn diagram to sort the data. Then determine how many students answered both bonus questions?
