

Math 130 - Quiz 7 IC

October 16, 2019

Name key

Score _____

Show all work to receive full credit. Supply explanations when necessary. You must work individually on this quiz.

1. (2.5 points) Use an appropriate formula to compute the exact value of $\cos(105^\circ)$.

$$\begin{aligned}\cos(105^\circ) &= \cos(60^\circ + 45^\circ) \\ &= \cos 60^\circ \cos 45^\circ - \sin 60^\circ \sin 45^\circ \\ &= \frac{1}{2} \left(\frac{\sqrt{2}}{2} \right) - \frac{\sqrt{3}}{2} \left(\frac{\sqrt{2}}{2} \right) \\ &= \frac{\sqrt{2}}{4} - \frac{\sqrt{6}}{4} = \boxed{\frac{\sqrt{2} - \sqrt{6}}{4}}\end{aligned}$$

2. (2.5 points) Use a sum or difference formula to rewrite $\sin\left(\frac{3\pi}{2} - \theta\right)$ as a trigonometric function of only θ .

$$\begin{aligned}\sin\left(\frac{3\pi}{2} - \theta\right) &= \sin \frac{3\pi}{2} \cos \theta - \cos \frac{3\pi}{2} \sin \theta \\ &= (-1) \cos \theta - (0) \sin \theta \\ &= \boxed{-\cos \theta}\end{aligned}$$

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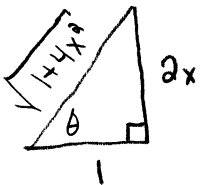
1. (3 points) Find the exact value of $\cos(165^\circ)$.

$$\begin{aligned} \cos(165^\circ) &= \cos(120^\circ + 45^\circ) = \cos 120^\circ \cos 45^\circ - \sin 120^\circ \sin 45^\circ \\ &= \left(-\frac{1}{2}\right) \frac{\sqrt{2}}{2} - \frac{\sqrt{3}}{2} \frac{\sqrt{2}}{2} \\ &= \frac{-\sqrt{2} - \sqrt{6}}{4} \end{aligned}$$

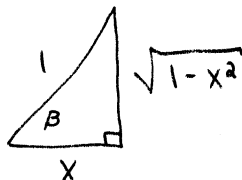
2. (5 points) Write as a algebraic expression:

$$\begin{aligned} &\sin(\arctan 2x - \arccos x) \\ &= \sin(\underbrace{\arctan 2x}_\theta) \cos(\underbrace{\arccos x}_\beta) - \cos(\underbrace{\arctan 2x}_\theta) \sin(\underbrace{\arccos x}_\beta) \\ &= \left(\frac{2x}{\sqrt{1+4x^2}}\right)(x) - \left(\frac{1}{\sqrt{1+4x^2}}\right)\left(\frac{\sqrt{1-x^2}}{1}\right) \\ &= \frac{2x^2 - \sqrt{1-x^2}}{\sqrt{1+4x^2}} \end{aligned}$$

$$\begin{aligned} \theta &= \tan^{-1} 2x \\ \tan \theta &= \frac{2x}{1} \end{aligned}$$



$$\begin{aligned} \beta &= \cos^{-1} x \\ \cos \beta &= \frac{x}{1} \end{aligned}$$



3. (4 points) Find all solutions in the interval $[0, 2\pi)$: $\cos(x + \pi) - \cos x - 1 = 0$

$$\cos x \cos \pi - \sin x \sin \pi - \cos x - 1 = 0$$

$$-\cos x - 0 - \cos x - 1 = 0$$

$$-2\cos x - 1 = 0$$

$$-2\cos x = 1$$

$$\cos x = -\frac{1}{2}$$

$$x = \frac{2\pi}{3}, \frac{4\pi}{3}$$

Turn over.

4. (3 points) Find all solutions: $\cos 2x + \cos x = 0$

$$2\cos^2 x - 1 + \cos x = 0$$

$$2\cos^2 x + \cos x - 1 = 0$$

$$(2\cos x - 1)(\cos x + 1) = 0$$

$$\cos x = \frac{1}{2} \quad \text{or} \quad \cos x = -1$$

$$x = \frac{\pi}{3}, \frac{5\pi}{3}$$

$$x = \pi$$

All solutions...

$$x = \frac{\pi}{3}, \frac{5\pi}{3}, \pi + 2k\pi, \text{ where } k \text{ is any integer}$$