

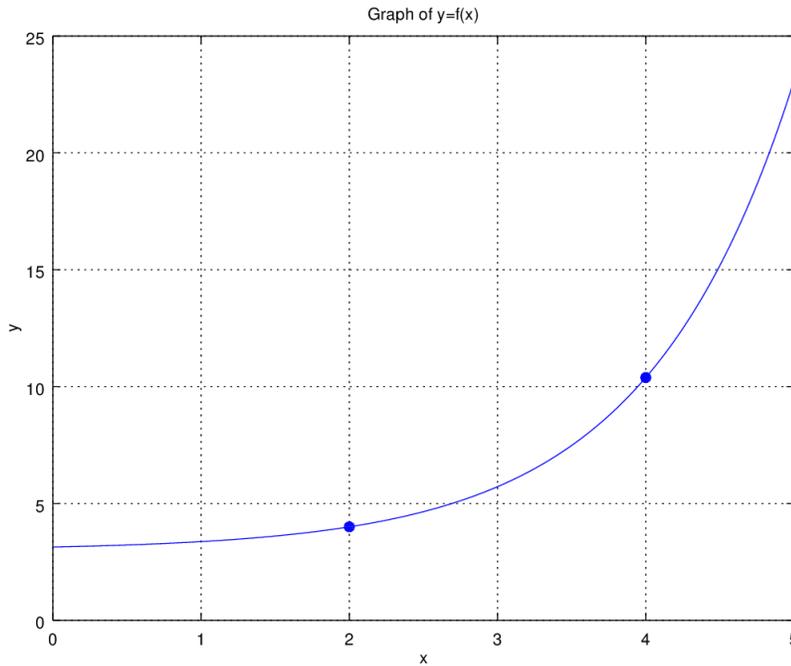
Math 131 - Test 2
March 12, 2020

Name _____

Score _____

Show all work to receive full credit. Supply explanations where necessary. Use differentiation rules for all derivatives, and do not simplify.

1. (6 points) The graph of $y = f(x)$ is shown below.

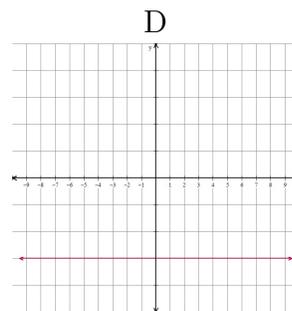
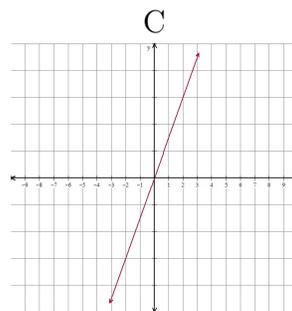
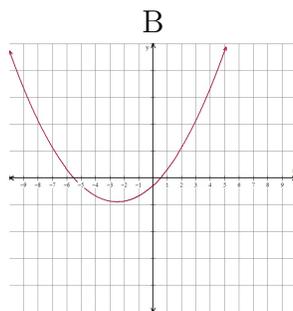
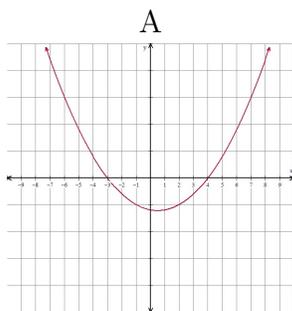
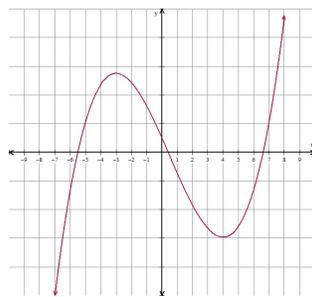


- (a) Sketch the secant line through the indicated points at $x = 2$ and $x = 4$. Let m be the slope of the secant line through those points. Estimate the value of m .
- (b) Which number is greatest: m , $f'(2)$, or $f'(4)$?. Explain your reasoning.
- (c) Which number is least: m , $f'(2)$, or $f'(4)$?. Explain your reasoning.

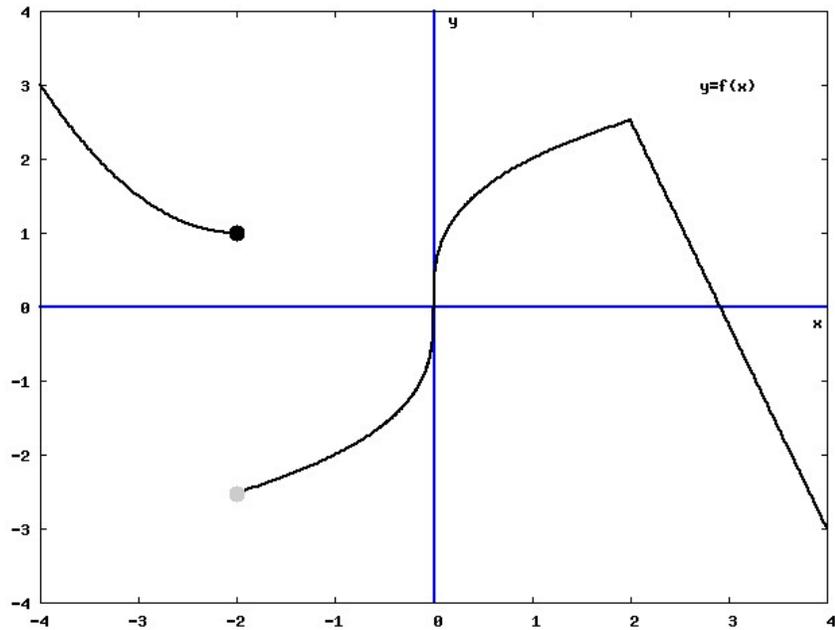
2. (4 points) Which one of the following best describes the line tangent to the graph of $f(x) = 5x^{1/3} - 2$ at the point $(0, -2)$? (Briefly explain, or show work, to receive full credit.)

- (a) The tangent line is horizontal.
- (b) The tangent line is vertical.
- (c) A unique tangent line does not exist.
- (d) The tangent line cannot be determined from the given information.

3. (5 points) The graph of $g(x)$ is shown below. Choose the lettered graph that best represents the graph of $g'(x)$. Explain your reasoning. Give at least two reasons to support your answer.



4. (6 points) The graph of $y = f(x)$ is shown below. Give the x -coordinates of three points at which $f'(x)$ does not exist. For each point, very briefly say why f' does not exist.



5. (5 points) Use the quotient rule to derive the formula for the derivative of $y = \cot x$.

6. Suppose you launch an object straight upward with a velocity of 64 ft/sec from over the edge of the top of an 80-ft building. Use the position function

$$s(t) = -16t^2 + v_0t + s_0,$$

where s represents height (in feet) at time t (in seconds), to solve the following problems.

- (a) (2 points) Determine the function that gives the object's height at time t .
- (b) (2 points) Determine the average rate of change the object's height over the interval from $t = 0$ to $t = 2$. (Include units with your answer.)
- (c) (2 points) Determine the function that gives the object's velocity at time t .
- (d) (2 points) Determine the object's velocity after 4 seconds. (Include units with your answer.)
- (e) (2 points) What is the acceleration of the object? (Include units with your answer.)
- (f) (4 points) Determine the object's maximum height. (Include units with your answer.)
- (g) (3 points) When does the object hit the ground?

7. (6 points) Use the derivative to determine each point (both coordinates) on the graph of $y = x^4 - 2x^2 + 3$ at which the tangent line is horizontal.

8. (6 points) Find an equation of the line tangent to the graph of $y = \frac{x^3 - 3x^2 + 4}{x^2}$ at the point where $x = 1$.

9. (7 points) Let $h(x) = \sqrt{x^4 + 9}$. Identify two functions, f and g , so that $h(x) = f(g(x))$. Then use the chain rule to determine $h'(x)$.

10. (6 points) Let $f(x) = 3x \sin x$. Find $f''(x)$.

11. (12 points) The table below gives the values of the functions f and g and their derivatives at selected values of x .

x	-2	-1	2
$f(x)$	1	3	-2
$f'(x)$	2	-1	-1
$g(x)$	2	0	-2
$g'(x)$	-3	-2	1

(a) If $h(x) = 4f(x) - 2g(x) + 5$, compute $h'(-1)$.

(b) If $h(x) = f(x) \cdot g(x)$, compute $h'(-1)$.

(c) If $h(x) = \frac{3f(x)}{g(x)}$, compute $h'(2)$.

12. (20 points) Differentiate. Do not simplify.

(a) $\frac{d}{dr} \left(7r^5 + 4r - 8\sqrt{r} + \frac{17}{r^2} \right)$

(b) $\frac{d}{dx} [(x^3 - x) \sec x]$

(c) $\frac{d}{dx} \cos(x^2 + 1)$

(d) $\frac{d}{dt} (2t + 1)^5 (3t - 2)^7$