Math 131 - Assignment 2

January 24, 2024

Name ______ Score _____

Show all work to receive full credit. Supply explanations when necessary. This assignment is due January 31.

1. Find the limit analytically:
$$\lim_{x \to -5} \left(\frac{x^2 + 3x - 10}{x^3 + 11x^2 + 30x} \right)$$

2. Find the limit analytically:
$$\lim_{x \to 1} \frac{\sqrt{x+3}-2}{x-1}$$

3. Find the limit analytically:
$$\lim_{w \to 0} \frac{(w+6)^2 - 36}{w}$$

4. Find the limit analytically:
$$\lim_{x \to 4} \frac{\frac{1}{2} - \frac{1}{x-2}}{x-4}$$

5. Explain why direct substitution cannot be used to evaluate the limit: $\lim_{x \to 1} \sqrt{1 - x^2}$

6. Find the limit analytically: $\lim_{y \to 0} \frac{\tan(6y)}{3y}$

7. Find the limit analytically:
$$\lim_{t \to 3^-} \frac{t^2 - t - 6}{|t - 3|}$$

8. Determine the value of the constant k so that $\lim_{x\to 4}\,g(x)$ exists.

$$g(x) = \begin{cases} kx + \sin(\pi x), & x \le 4\\ x\cos(\pi x) - x^2, & x > 4 \end{cases}$$

9. Find the limit analytically: $\lim_{x \to -2^+} (5x^2 - 10x + 13)$

10. Give an example of a one-sided limit that does not exist and say why.