

Math 171 - Quiz 5

September 30, 2010

Name key

Score _____

Show all work to receive full credit. Supply explanations when necessary.

1. (2 points) The following table gives information about the functions f and g .

x	$f(x)$	$f'(x)$	$g(x)$	$g'(x)$
0	-7	0	4	2
1	-8	-1	7	5
2	-7	4	DNE	DNE
3	2	15	1	5

Use this information to find an equation of the line tangent to the graph of $y = f(x)g(x)$ at the point where $x = 1$.

$$\frac{dy}{dx} = f'(x)g(x) + f(x)g'(x)$$

$$y - y_0 = m(x - x_0)$$

$$\left. \frac{dy}{dx} \right|_{x=1} = (-1)(7) + (-8)(5) = -7 - 40 = -47$$

$$y + 56 = -47(x - 1)$$

$$y = -47x - 9$$

$$y|_{x=1} = f(1)g(1) = -56$$

2. (3 points) An object is thrown straight up from over the side of a 110-ft building. If the object's initial velocity is 50 ft/sec, how high will it go and when will it land on the ground.

$$s(t) = -16t^2 + 50t + 110$$

$$s(t) = 0$$

$$s'(t) = -32t + 50$$

$$\Rightarrow t = \frac{-50 \pm \sqrt{50^2 + 4(16)(110)}}{-32}$$

$$s'(t) = 0 \Rightarrow t = \frac{50}{32} = 1.5625$$

$$\Rightarrow t = 4.6148$$

$$s(1.5625) = 149.0625$$

IT WILL LAND ON THE GROUND AFTER

4.6148 SEC

THE OBJECT WILL REACH A HEIGHT OF 149.0625 FT.

3. (1 point) Find $f''(x)$ if $f(x) = 8 \sec x$.

$$f'(x) = 8 \sec x \tan x$$

$$\begin{aligned} f''(x) &= 8 \sec x (\sec^2 x) + 8 (\sec x \tan x) \tan x \\ &= \boxed{8 \sec^3 x + 8 \sec x \tan^2 x} \end{aligned}$$

4. (3 points) Find each derivative.

$$\begin{aligned} \text{(a)} \quad \frac{d}{dx} \tan(3\pi x^2) &= \sec^2(3\pi x^2) (6\pi x) \\ &= \boxed{6\pi x \sec^2(3\pi x^2)} \end{aligned}$$

$$\begin{aligned} \text{(b)} \quad \frac{d}{dr} \sin^2(2\pi r + 1) &= 2 \sin(2\pi r + 1) \frac{d}{dr} \sin(2\pi r + 1) \\ &= \boxed{2 \sin(2\pi r + 1) \cos(2\pi r + 1) (2\pi)} \end{aligned}$$

5. (1 point) Find the rate of change of $g(x) = \frac{\sqrt{x} + 6}{x^2 - 5x}$ at the point $(4, -2)$.

$$g'(x) = \frac{(x^2 - 5x) \frac{1}{2} x^{-1/2} - (\sqrt{x} + 6)(2x - 5)}{(x^2 - 5x)^2}$$

$$g'(4) = \frac{(-4)\left(\frac{1}{4}\right) - (8)(3)}{16} = \boxed{\frac{-25}{16}}$$