

Math 171 - Quiz 10

November 20, 2014

Name key

Score _____

Show all work to receive full credit. Supply explanations when necessary.

1. (5 points) Use 4 subintervals of equal length and subinterval midpoints to compute a Riemann sum for $g(x) = x^2 + x$ on the interval $[0, 2]$.

$$\Delta x = \frac{2-0}{4} = \frac{1}{2}$$

$$\text{PARTITION: } 0 < 0.5 < 1 < 1.5 < 2$$

$$c_k \text{'s: } 0.25, 0.75, 1.25, 1.75$$

$$\begin{aligned} \text{RIEMANN SUM} &= 0.5 \left[g(0.25) + g(0.75) + g(1.25) + g(1.75) \right] \\ &= \boxed{4.625} \end{aligned}$$

2. (5 points) Let $f(x) = \frac{1}{x}$. Use 5 subintervals of equal length to compute a Riemann sum for f over the interval $[1, 2]$.

$$\Delta x = \frac{2-1}{5} = \frac{1}{5}$$

$$\text{PARTITION: } 1 = \frac{5}{5} < \frac{6}{5} < \frac{7}{5} < \frac{8}{5} < \frac{9}{5} < \frac{10}{5} = 2$$

$$c_k \text{'s: } \frac{11}{10}, \frac{13}{10}, \frac{15}{10}, \frac{17}{10}, \frac{19}{10}$$

$$\begin{aligned} \text{RIEMANN SUM} &= \frac{1}{5} \left[\frac{10}{11} + \frac{10}{13} + \frac{10}{15} + \frac{10}{17} + \frac{10}{19} \right] \\ &= \boxed{\frac{479378}{692835} \approx 0.6919} \end{aligned}$$