If the right-hand side of the equation

$$
\frac{d y}{d x}=f(x, y)
$$

can be expressed as a function of the ratio $y / x$ alone, then we say the equation is homogeneous.

In this context, homogeneous means that the $x$ and $y$ variables have a balanced presence.

In a homogeneous equation, the substitution

$$
u=\frac{y}{x}, \quad \frac{d y}{d x}=u+x \frac{d u}{d x}
$$

will reduce it to a separable equation.

