Math 233-Quiz 5
September 28, 2023

Name $\qquad$
Score $\qquad$

Show all work to receive full credit. Supply explanations when necessary.

1. (2 points) Let $\vec{r}(t)=t^{2} \hat{\imath}+t^{3} \hat{\jmath}+t \hat{k}$. Compute $\hat{T}(t)$.
2. (3 points) What are the three important characteristics of the unit tangent vector?
3. (4 points) Let $\vec{r}(t)=\left(4 t^{2}+3\right) \hat{\imath}+5 \hat{\jmath}+\left(t^{2}+7\right) \hat{k}$. Reparameterize $r$ in terms of the arc length parameter starting from $t=0$.
4. (1 point) Let $\vec{R}(s)$ be your reparameterization above. What is the magnitude of $\vec{R}^{\prime}(s)$ ?
