Math 233 - Quiz 4

February 16, 2023

Name ________

Show all work to receive full credit. Supply explanations when necessary.

1. (5 points) Find the function $\vec{r}(t)$ that satisfies

$$\vec{r}'(t) = e^{-2t} \hat{i} - t \hat{j} + \frac{5t}{t^2 + 1} \hat{k}; \qquad \vec{r}(0) = 5\hat{i} + 3\hat{j} - 2\hat{k}.$$

2. (3 points) Let $\vec{r}(t) = \sin 6t \,\hat{\imath} + \cos 6t \,\hat{\jmath} + 8t \,\hat{k}$. Compute $\hat{T}(t)$.

3. (2 points) What are the three important characteristics of the principal unit tangent vector.