Math 240 - Quiz 5
February 23, 2023

Name $\qquad$
Score $\qquad$

Show all work to receive full credit. Supply explanations when necessary.

1. (5 points) Solve: $\quad y^{\prime \prime}-3 y^{\prime}-10 y=0 ; \quad y(0)=3, y^{\prime}(0)=-4$
2. (4 points) Solve: $y^{\prime \prime \prime}-8 y^{\prime \prime}+16 y^{\prime}=0$
3. (1 points) It is easy to verify that $y_{1}(x) \equiv 1$ and $y_{2}(x)=\ln x$ are linearly independent solutions of $y^{\prime \prime}+\left(y^{\prime}\right)^{2}=0$. It is also easy to verify that $y(x)=c_{1} y_{1}(x)+c_{2} y_{2}(x)$ is, in general, NOT a solution. Explain why the linear combination of solutions is not a solution.
