

Pascal's Triangle

$$\begin{array}{cccccccc} & & & & 1 & & & & \\ & & & & 1 & & 1 & & \\ & & & 1 & 2 & & 1 & & \\ & & 1 & 3 & 3 & 1 & & & \\ & 1 & 4 & 6 & 4 & 1 & & & \\ 1 & 5 & 10 & 10 & 5 & 1 & & & \\ 1 & 6 & 15 & 20 & 15 & 6 & 1 & & \\ 1 & 7 & 21 & 35 & 35 & 21 & 7 & 1 & \\ 1 & 8 & 28 & 56 & 70 & 56 & 28 & 8 & 1 \end{array}$$

The coefficients of $(x+y)^n$ can be obtained from the $(n+1)^{\text{st}}$ row of Pascal's Triangle.

For example:

$$(x+y)^4 = x^4 + 4x^3y + 6x^2y^2 + 4xy^3 + y^4$$

$$(x-y)^3 = x^3 - 3x^2y + 3xy^2 - y^3$$

Quadratic Formula

$$ax^2 + bx + c = 0 \iff x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Completing the Square

$$ax^2 + bx + c = a \left(x + \frac{b}{2a} \right)^2 + \left(c - \frac{b^2}{4a} \right)$$

Special Factors

$$A^2 - B^2 = (A - B)(A + B)$$

$$A^3 - B^3 = (A - B)(A^2 + AB + B^2)$$

$$A^3 + B^3 = (A + B)(A^2 - AB + B^2)$$

$$A^4 - B^4 = (A + B)(A - B)(A^2 + B^2)$$

Logarithms

$$\log_a 1 = 0$$

$$\log_a a^x = x$$

$$\log_a xy = \log_a x + \log_a y$$

$$\log_a \frac{x}{y} = \log_a x - \log_a y$$

$$\log_a x^y = y \log_a x$$

$$\log_a x = \frac{\log_b x}{\log_b a}$$

Absolute Value

$$|x| = \begin{cases} x & \text{if } x \geq 0 \\ -x & \text{if } x < 0 \end{cases}$$

$$|-x| = |x|$$

$$|xy| = |x| \cdot |y|$$

$$\left| \frac{x}{y} \right| = \frac{|x|}{|y|}$$

$$|x|^2 = x^2$$

$$\sqrt{x^2} = |x|$$

$$|x| = p \iff x = -p \text{ or } x = p$$

$$|x| < p \iff -p < x < p$$

$$|x| > p \iff x < -p \text{ or } x > p$$

Triangle Inequality

$$|x + y| \leq |x| + |y|$$

Lines

$$\text{Slope: } m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$\text{Point-Slope Form: } y - y_1 = m(x - x_1)$$

$$\text{Slope-Intercept Form: } y = mx + b$$

$$\text{Standard Form: } Ax + By = C$$

$$\text{Vertical Lines: } x = a$$

$$\text{Horizontal Lines: } y = b$$

Distance Formula

$$D = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

Midpoint Formula

$$\left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$$

Inverse Functions

$$y = f(x) \iff x = f^{-1}(y)$$

Compound Interest

$$n \text{ times per year: } A = P \left(1 + \frac{i}{n} \right)^{nt}$$

$$\text{Continuously: } A = Pe^{it}$$